

# Quantum Mechanical States

- Two versions of the Schrödinger eqn.  
dependent & time-independent

- Picked  $\psi(x)$  over  $\psi(p)$

-  $t$  &  $E$  are related by Fourier-Transform

\* Meaning of the Wave function: see postulate 4

In QM; eigenvalues are obtained (an exact number), but this number will change every "scan". The probability of obtaining a value can be obtained

See  $x/p$  plot from lecture notes:

takeaway

$\Delta x \Delta p = \hbar/2$  does not limit accuracy when calculating  $x$

[  $\psi(x) = f(x-x_n)$  ]  
any value of momentum is possible

A molecule is in a state  $\psi(x, t)$ .

We have an observable (could be anything)  $A$  which has an operator " $\hat{A}$ "

- what are values of  $A$  that can be measured?

If  $\hat{A}$  has eigenvalues  $a_n$  and eigenfunction  $\psi_n(x) \Rightarrow a_n$  are the only values that can be measured, with probability

$$P(A=a_n \text{ @ time } t) = \left| \int_{-\infty}^{\infty} \psi_n^*(x) \cdot \psi(x, t) dx \right|^2$$

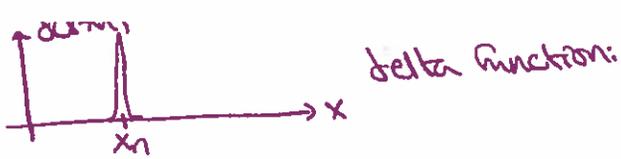
Multiply vector  $x$  or matrix and you get a multiple of the matrix back, that was an eigenvector

-  $x^2$  is not an eigenfunction of  $\partial/\partial x$

-  $e^{-x}$  is an eigenfunction of  $\partial/\partial x$   
eigenvalue is  $-1$

If  $\psi(x)$  looks very different from  $\psi(x, t)$  then the integral is not going to be 0

If state of system looks like the state of the observable, you will obtain values



delta function:

Example: observable is position

$$\hat{A} = \text{position } x \Rightarrow \hat{A} = x \Rightarrow x \psi_n(x) = x_n \psi_n(x)$$

$$\psi_n = \delta(x-x_n), = x_n \delta(x-x_n) \begin{cases} \text{if } x \neq x_n \delta(x-x_n) = 0 \\ \text{and } x \cdot 0 = x_n \cdot 0 \\ \text{if } x = x_n; \delta(x-x_n) \neq 0 \\ \text{and } x_n(\delta(x-x_n)) = x_n \delta(x-x_n) \end{cases}$$

true for all values of  $x$

$$\Rightarrow P(x = x_n \text{ attained})$$

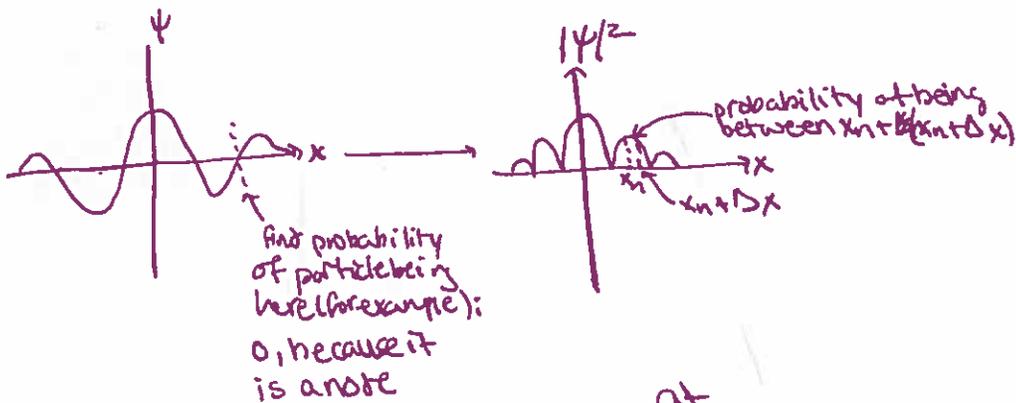
$$= \left| \int_{-\infty}^{\infty} dx \delta(x-x_n) \psi(x,t) \right|^2 \quad \text{if } x \neq x_n \Rightarrow \delta(x-x_n) = 0 \text{ value is } 0$$

$$= |\psi(x_n, t)|^2$$

$$= \psi^*(x,t) \cdot \psi(x,t) \geq 0 \text{ real}$$

(negative probabilities don't make sense)

$|\psi(x_n, t)|^2$  is the probability that the molecule is at position  $x_n$  and time  $t$



Probability of finding the particle <sup>at</sup> all values of  $x$  is 1

$$\Rightarrow \int_{-\infty}^{\infty} dx |\psi(x,t)|^2 = 1 = \int_{-\infty}^{\infty} dx \psi^*(x,t) \psi(x,t)$$

Normalization of a wavefunction