

Last time, we saw that there are special wavefunctions, of the form

$$\Psi(x,t) = \Psi_n(x) \exp(-iE_n t/\hbar)$$

whose probability is stationary (does not change with time).

The wavefunctions  $\Psi_n(x)$  must be solutions of the time-independent Schrödinger equation

$$H\Psi_n(x) = E_n \Psi_n(x)$$

where  $E_n$  is the exact energy of the particle when its wavefunction is  $\Psi(x,t) = \Psi_n(x) \exp(-iE_n t/\hbar)$ .

For a vibrating molecule (harmonic oscillator), we used a symmetry argument to prove that the Gaussian is an eigenstate with energy  $E_0 = \hbar\omega/2$  if mass  $m$  and force constant  $k$  are equal to 1.

Today: does the time-independent Schrödinger equation have more than one stationary state, unlike classical mechanics?

