

Lecture 5

Wednesday, August 30, 2023 10:01 AM

Postulates of QM

Definitions =

$$\textcircled{1} \text{ Hamiltonian } H = E = \overset{\text{KE}}{\frac{p^2}{2m}} + \overset{\text{PE}}{V(x)}$$

$\textcircled{2}$ Conjugate variables are related by a derivative =

$$\overset{\text{operator}}{\hat{a}} = \frac{c}{2\pi i} \frac{\partial}{\partial b} \Rightarrow \Delta a \Delta b = \frac{c}{4\pi}$$

(music: $c=1$, QM: $c=h$)

$\textcircled{3}$ operator = something that acts on a function

ex. function = $\psi(x)$; operator = S . $\Rightarrow S \cdot \psi(x) = S\psi(x)$

" " ; operator = $\frac{\partial}{\partial x} \Rightarrow \frac{\partial}{\partial x} \psi(x) = \frac{\partial \psi}{\partial x}$

multiplication & derivative operator

In Class Exercise

Frequency operator: $\hat{v} = \frac{1}{2\pi i} \frac{\partial}{\partial t}$; What does the operator

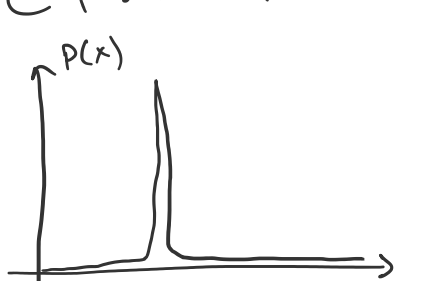
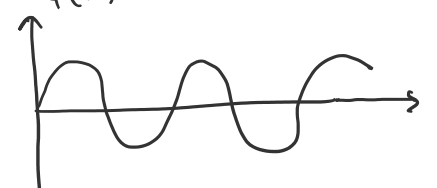
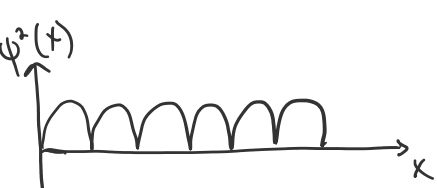
\hat{v}^2 do to the function $\psi = \sin(2\pi\nu t)$?

$$\hat{v}^2 = \frac{-1}{4\pi^2} \frac{\partial^2}{\partial t^2}$$

$$\hat{v}^2 \psi = \frac{-1}{4\pi^2} \frac{\partial^2}{\partial t^2} (\sin(2\pi\nu t)) = \frac{(2\pi\nu)^2}{4\pi^2} \sin(2\pi\nu t) = \nu^2 \underbrace{\sin(2\pi\nu t)}_{\text{eigenfunction}} = \hat{v}^2 \underbrace{\sin(2\pi\nu t)}_{\text{eigenfunction}}$$

In QM, apply operators to functions, get values of variables

Postulates =

CM	QM
<p>$\textcircled{1}$ x & p are independent</p>	<p>$\textcircled{1}$ $\hat{p} = \frac{h}{2\pi i} \frac{\partial}{\partial x}$ x & p are conjugate</p>
<p>$\textcircled{2}$ Equation of motion</p> $-\frac{\partial V}{\partial x} = F = ma = m \frac{\partial^2 x}{\partial t^2}$	<p>$\textcircled{2}$ $\hat{H} \psi(x,t) = i \frac{\partial}{\partial t} \psi(x,t)$</p>
<p>$\textcircled{3}$ Probability of finding particles. Particles can be found exactly @ position x</p>  <p>average $\bar{A} = \int dx P(x) A(x)$</p>	<p>$\textcircled{3}$ The probability $P(x) = \psi(x) ^2 \geq 0$</p>   $\bar{A} = \int dx \psi^*(x) A(x) \psi(x)$ <p> $z = x + iy$ $z z^* = x^2 + y^2$ $z^* = x - iy$ $z ^2 = x^2 + y^2 = r^2$ </p>
<p>$\textcircled{4}$ Doesn't exist</p>	<p>$\textcircled{4}$ There are 2 kinds of particles w/ "spin"</p> <p>Boson = $s = 0, 1, 2, \dots$</p> <p>Fermions = $s = \frac{1}{2}, \frac{3}{2}, \dots$</p>